## Analytic Geometry - Assignment \#3

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Exercise 1 Let $r$ be the straight line through $A=(1,2,5)$ and $B=(0,1,0)$. Find the coordinates of a point $P$ on $r$ with the length of $\overrightarrow{P B}$ being three times the length of $\overrightarrow{P A}$.

Exercise 2 Prove that the locus of all points that are equidistant from $A=(1,-1,2)$ and $B=(4,3,1)$ is a plane $\pi$. Prove that $\pi$ is perpendicular to line segment AB.

Exercise 3 Let $r$ and $s$ be skew lines through $A=(0,1,0)$ and $B=(1,1,0)$ and through $C=$ $(-3,1,-4)$ and $D=(-1,2,-7)$, respectively. Find the equation of the line $t$ intersecting both $r$ and $s$, and parallel to the vector $\vec{v}=(1,-5,-1)$.

Exercise 4 Prove that the line $r$ is contained in the plane $\pi$, where $r: x=-1+m, y=-1+m, z=3 m$ and $\pi: x+2 y-z+3=0$.

Exercise 5 Find the symmetric point $P^{\prime}$ for the point $P=(2,1,0)$ with respect to the line $r: x=$ $1+t, y=2-t, z=1+t$.

Exercise 6 Find the asymptotes for the hyperbola $4 y^{2}-x^{2}=1$.

